

Cohesive zone modelling of Mode III delamination using the edge crack torsion test

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ABSTRACT

In the experimental studies of mode III delamination using the edge crack torsion test, the crack initiation and propagation measurement are always difficult. This information could be obtained through numerical modelling. The objective of this study is to propose a guideline to model mode III delamination behaviour using cohesive elements. Finite element models of an edge crack torsion specimen were developed based on the data from the literature. The delamination behaviour of the specimen along the pre-crack, which was located at the mid-thickness location, was modelled using cohesive elements. Through parametric studies, it was found that for reliable numerical modelling, a mesh size of 0.5 mm was suggested, which provided three elements in the cohesive zone. As for the interface strength, it was recommended to choose 80 MPa. In addition, a viscosity parameter of 1×10^{-3} was found to be a good choice for reasonable computational time and converged numerical results. Besides, the interface stiffness was suggested to be 4×10^6 MPa/mm. Furthermore, the fracture process zone contour revealed that the delamination was started at a normalised location of approximately 0.7. Not only that, the fracture energy and strain distribution plots have shown the delamination was mode III dominated within the normalised distance of 0.34-0.86. The results from this study suggested that cohesive zone modelling is a useful method for the detailed analysis of the mode III delamination of an ECT specimen. The numerical modelling approach suggested from this study could be applied to ECT specimens at various different initial crack lengths. It also has the potential to be used to simulate the mode III delamination of other various types of laminated composites.

Keywords: Interlaminar fracture; Mode III; edge crack torsion; cohesive zone modelling.

INTRODUCTION

In the studies of the delamination of composite laminates, mode III delamination has been recognised to be important due to its contribution to edge delamination [1]. The recent testing methods on mode III delamination include the modified split cantilever beam (MSCB) [2, 3], modified edge crack torsion (MECT) (which is still commonly known as edge crack torsion (ECT)) [4, 5], six ECT (6ECT) [6], modified shear torsion bending (MSTB) [7], which was initially designed for mixed-mode I+II+III delamination [8], split-shear torsion (SST) [9] and newly designed torsional tests [10]. Among the above

mentioned tests, the edge crack torsion test is currently under evaluation by the American Society for Testing and Materials (ASTM) to be standardised [11]. The advantages of the edge crack torsion test include pure mode III delamination in the middle region of the specimen and negligible friction between the delaminated surfaces [12]. However, during the experimental testing, the initiation and propagation of the crack of the edge crack torsion specimen are not easily captured from the edges. This information could be obtained through numerical analyses.

The common numerical modelling approaches for the delamination of composite laminates are the virtual crack closure technique (VCCT) and the cohesive zone model (CZM) [13]. The VCCT has been commonly employed by various researchers to simulate the mode III delamination of carbon/epoxy [6, 14-16] and glass/epoxy [3, 5, 17-20] composite laminates. Nevertheless, in recent years, the CZM has gained its popularity in simulating the delamination behaviour of laminated composites. Its major advantage over the VCCT is the ability to predict both the onset and non-self-similar propagation of delamination without needing a pre-crack [21]. However, the CZM has been used more widely encountered in simulating mode I, mode II and mixed-mode I+II delamination behaviour [22-24]. It is comparatively less common to be employed in mode III delamination [6, 25, 26]. Furthermore, in the above mentioned three references, the choice of the cohesive parameters (element size, interface strength, viscosity parameter and interface stiffness) was not described. In this respect, there is a need to conduct a detailed parametric study of the cohesive parameters on mode III delamination of the edge crack torsion (ECT) specimen. The objective of this study is to suggest guidelines to select a suitable range for the cohesive parameters to simulate the delamination behaviour of the ECT specimens. The experimental result from the literature [15] was used. Through parametric studies, guidelines for the parameter selection for mode III delamination using the ECT test were proposed. Subsequently, the damage initiation and propagation profiles were also plotted and compared with the fracture energy distribution. Finally, the strain distributions in the ECT specimen were presented.

NUMERICAL MODELLING

Cohesive Zone Model for Pure Tearing Mode Failure

In this study, a cohesive element [27] was employed to simulate the delamination between the plies adjacent to the pre-crack. This type of element considers only out-of-plane stress components, and is generally known as the interface element. Since the present study focused on the mode III interlaminar fracture, only the formulation for delamination in the tearing mode is discussed. Consider an eight-node three-dimensional cohesive element that is subjected to loading as shown in Figure 1. Before any delamination damage occurs, the traction separation behaviour is assumed to be linear elastic. At any instant, the element is experiencing a relative displacement between the upper, $u_{III,up}$ and lower, $u_{III,low}$ nodes, which is denoted as δ_{III} and is stored as the corresponding displacement at the integration point. For uncoupled shear traction, the constitutive behaviour is given as:

$$t_{III} = k_{III} \delta_{III} \quad (1)$$

where t_{III} is the traction (stress) and k_{III} is the interface stiffness (stiffness per unit thickness of the cohesive element). The subscript *III* refers to the tearing mode.

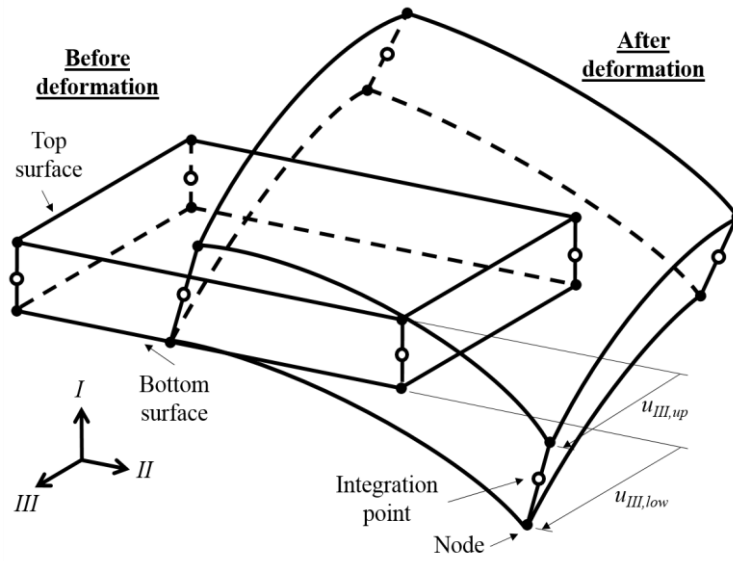


Figure 1. Schematic diagram of a three-dimensional cohesive element.

Interface damage initiation is governed by a quadratic nominal stress criterion. For pure mode III, it is written as:

$$\left\{ \frac{t_{III}}{t_{u,III}} \right\}^2 = 1 \quad (2)$$

where $t_{u,III}$ is the interlaminar strength in the tearing direction, which could be reduced to the maximum nominal stress criterion for this particular case, where the traction ratio on the left is not squared.

Delamination starts to occur at a material point of the interface when the quotient of the nominal stress ratio reaches unity. Subsequently, damage evolution occurs. In this study, the linear damage evolution law was used as described in Figure 2.

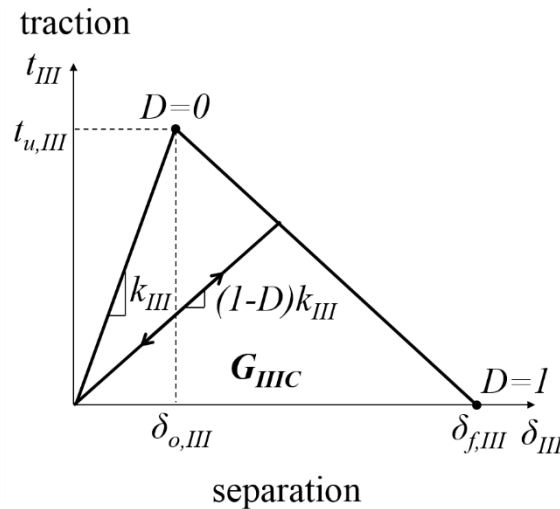


Figure 2. Schematic diagram of the bilinear traction separation law.

The damage parameter, D for the linear softening behaviour is written as:

$$D = \frac{\delta_{f,III} (\delta_{III} - \delta_{o,III})}{\delta_{III} (\delta_{f,III} - \delta_{o,III})} \quad (3)$$

where $\delta_{o,III}$ and $\delta_{f,III}$ refer to the relative displacement at damage onset and total failure. Linear softening was adopted due to its simplicity and accuracy compared to other traction-separation laws such as the exponential law [27].

During damage evolution, the constitutive behaviour of the interface is then calculated based on the following equation:

$$t_{III} = (1 - D)k_{III}\delta_{III} \quad (4)$$

The damage evolution zone is governed by the dissipated energy due to damage, which is represented by the area under the curve of traction-separation. With the computed relative displacement δ_{III} at each iteration, D could be calculated. The damage variable, D is then updated into the stiffness matrix in Equation (4) and the traction, t_{III} is updated. Subsequently, the corresponding mode III fracture energy, G_{III} could be calculated and compared with G_{IIIc} . When the total fracture energy is equivalent to the fracture toughness ($G_{III} = G_{IIIc}$), $D = 1$ and the material point is completely damaged.

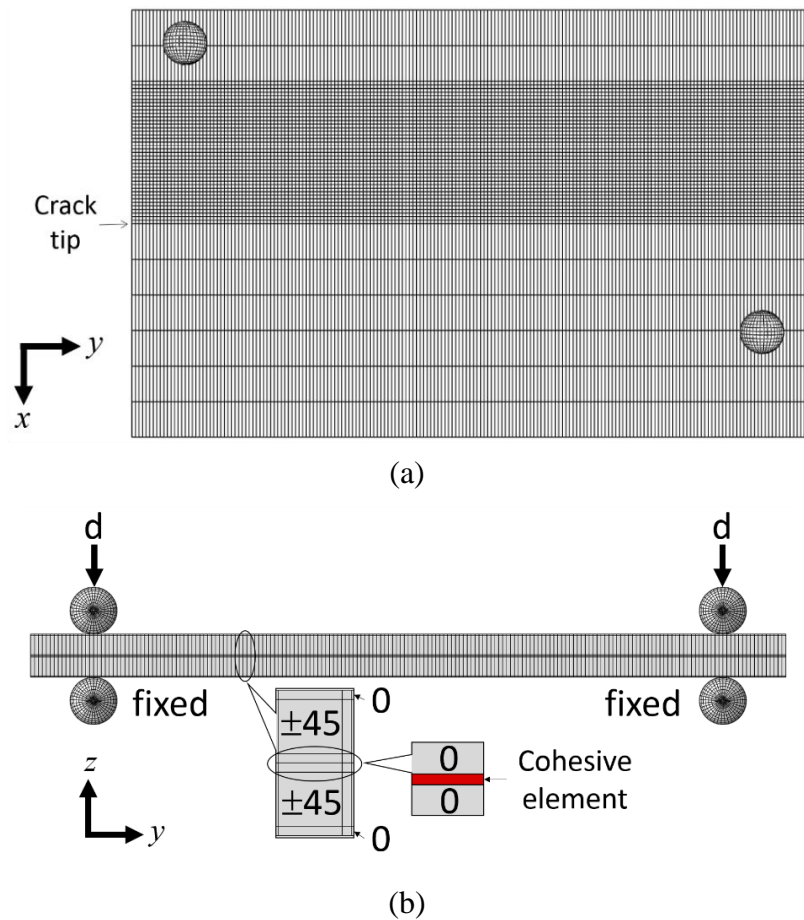


Figure 3. Finite element model of the ECT specimen: (a) top view; (b) front view.

Finite Element Modelling

The finite element models were developed based on the information from the literature [15]. The material was a Texipreg T300/HS 160 REM carbon/epoxy composite with the lamina properties listed in Table 1 below. Figure 3 shows the finite element model of the ECT specimen, with the stacking sequence of $[0/(-45)_4/(+45)_4/0]_s$. The two bottom spheres were fixed and the vertical displacement was imposed by the two upper spheres. The two mid- and outer-ply (0 plies) were modelled as single layers, whereas all other 45 plies were modelled by one element in the thickness direction. The composite layers were modelled using 8-node continuum shell elements (SC8R). As for the mid-plane interface, 8-node cohesive elements (COH3D8) were prescribed to simulate the delamination behaviour. Cohesive elements were modelled with 1 μm thickness in order to avoid interpenetration [28]. The input for the pure-mode fracture toughness for cohesive elements were $G_{IC} = 0.25 \text{ N/mm}$, $G_{IIC} = 0.8 \text{ N/mm}$ and $G_{IIIC} = 0.9 \text{ N/mm}$ [15].

Table 1. Lamina properties of the Texipreg T300/HS 160 REM carbon/epoxy composite[15].

E_1 (GPa)	E_2 (GPa)	G_{12} (GPa)	G_{13} (GPa)	G_{23} (GPa)	ν_{12}
130.0	8.2	4.1	4.1	4.1	0.27

Guidelines of Cohesive Parameter Selection

The four parameters necessary to be considered for accurate cohesive zone modelling are element size (l_e), interface strength ($t_{u,III}$), viscosity parameter (D_v) and interface stiffness (k_{III}). The descriptions of the following parameters and their selection are as follows:

The element size, l_e is an important parameter because a refined enough mesh in the cohesive zone allows for the accurate prediction of the traction in front of the crack tip. Based on the past studies using three-dimensional cohesive elements, researchers generally chose element size between 0.125-1 mm [29, 30]. A larger range of 0.25-2.5 mm of mesh size was considered in this study for a reasonable computational time. The interface strength is influenced by the resin strength [22]. A relatively high but lower than the physical value should be taken for an improved simulation at a relatively coarser mesh [29]. The parametric study was performed in the range of the tensile strength of the epoxy (40-100 MPa) [31]. This is also the same range of values used by various researchers as summarised earlier [22]. Viscous regularisation is introduced in order to avoid the termination of the computational routine due to the numerical instability caused by material softening behaviour. An appropriate value of the viscosity parameter improves the convergence of the analysis, but does not compromise the results to a notable extent. Hence, it is essential to choose an optimised viscosity parameter to obtain convincing results. A range from 1×10^{-6} to 1×10^{-1} was found from the literature [22, 32, 33]. In this study, a smaller range of the viscosity parameter between 1×10^{-5} - 1×10^{-2} was considered.

Interface stiffness is basically not a physical parameter [22], since the out-of-plane stiffness of a very thin layer is not feasible to be characterised through experiments. In this study, the approach shown by Equation (5) was adopted, where E_m is Young's modulus of the resin (taken as 4 GPa based on the range 3-6 GPa [31]) and h_{ce} is the thickness of the cohesive element (1 μm). This approach is similar to the one mentioned by Allix and Blanchard [34] except that they used out-of-plane stiffness E_3 instead of E_m . This study used E_m because both E_3 and E_m are usually falling in the similar range, and E_m is much easier to be determined experimentally. For E_3 , this is generally assumed to be equal to E_2 . Thus, the initial estimation of k_{III} was $4 \times 10^6 \text{ MPa/mm}$. This is in the similar

range of the values generally used by researchers [22, 29, 30, 35]. To study the effects of interface stiffness on the numerical force-displacement response, the range between 4×10^5 - 4×10^8 MPa/mm was considered. Table 2 summarises the range of the cohesive parameters considered in this study.

$$k_{III} = \frac{E_m}{h_{ce}} \quad (5)$$

Table 2. Parametric studies of the cohesive parameters.

Cohesive parameters	Range
Element size, l_e	0.25-2.5 mm
Interface strength, $t_{u,III}$	40-100 MPa
Viscosity parameter, D_v	1×10^{-5} - 1×10^{-2}
Interface stiffness, k_{III}	4×10^5 - 4×10^8 MPa/mm

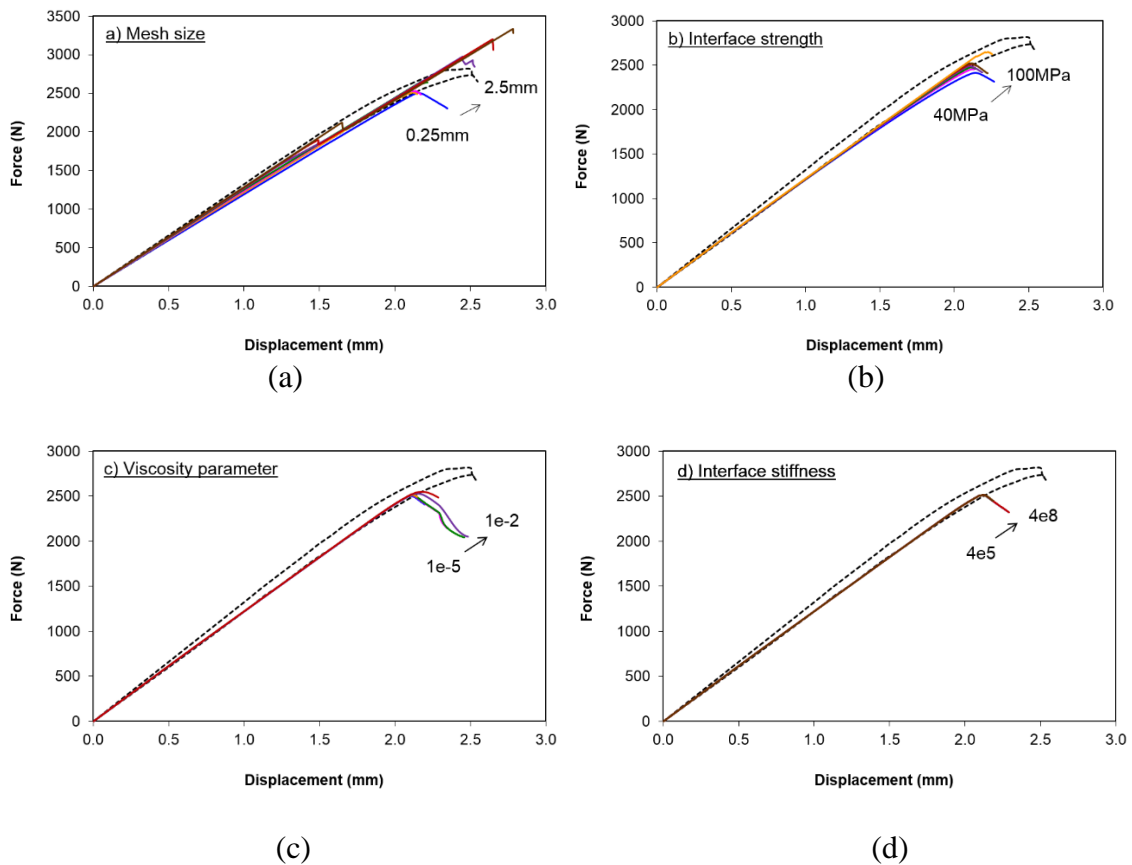


Figure 4. Influence of (a) mesh size; (b) interface strength; (c) viscosity parameter and (d) interface stiffness on the force-displacement responses.

RESULTS AND DISCUSSION

Influence of Cohesive Parameters

Figure 4 compares the experimental and numerical force-displacement curves of the ECT specimen. It could be observed from Figure 4(a)-(d) that the cohesive parameters had a

negligible effect on the slope of the force-displacement curves. Nevertheless, a certain variation was found in the peak load. Figure 4(a) illustrates that the peak load increased with the mesh size. Specifically, when the mesh size was 1.5 mm and above, the numerical peak loads have exceeded the experimental ones. As for the interface strength, this was also reported to follow an increasing trend (Figure 4(b)). Up to 100 MPa, the numerical to experimental peak load ratio was 0.94. In addition, Figure 4(c) indicates that the increasing viscosity parameter has increased the numerical peak load as well. Similar to the interface strength, the numerical peak loads were always lower compared to the experimental values. A slight increment in the numerical peak load was noticed with the increment in the interface stiffness (Figure 4(d)). However, the difference was negligible. The detailed comparison among the numerical peak loads was therefore carried out in the following.

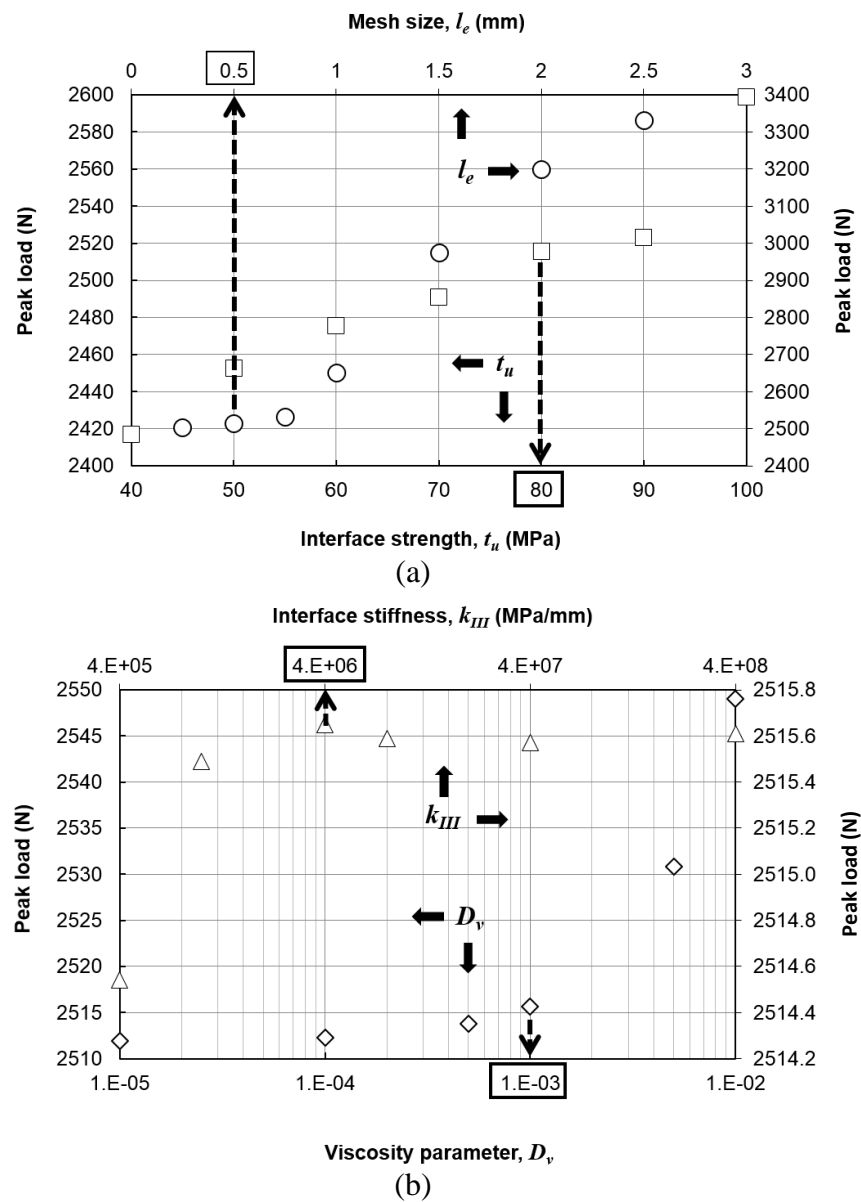


Figure 5. Comparison between the (a) mesh size and interface strength; and (b) viscosity parameter and interface stiffness on the numerical peak loads.

From Figure 5(a), it was found that a mesh size of 0.5 mm and below is recommended. In addition, the interface strength was noticed to converge up to 80 MPa. As for the viscosity parameter, Figure 5(b) depicts that a value of 1×10^{-3} and below was a good choice for the converged result. A further decrement in the viscosity parameter did not vary the numerical peak load for more than 1%; however, it would significantly increase the computation time. This was similar to a recent study on the three-dimensional modelling of mode II delamination using the CZM [36]. Furthermore, the interface stiffness did not seem to be sensitive within the studied range. This was because the initial linear elastic region of the traction-separation response was relatively small compared to the damage propagation region. Hence, the value of 4×10^6 MPa/mm was a good choice because it could be easily estimated using Equation (5). This was also in the similar range of the values generally used by researchers [22, 29, 30, 35]. From the above parametric studies, the suggested cohesive parameters for accurate simulation with reasonable computational time were $l_e = 0.5$ mm, $t_{u,III} = 80$ MPa, $D_v = 1 \times 10^{-3}$ and $k_{III} = 4 \times 10^6$ MPa/mm. This set of cohesive parameters was found to be within the similar range as suggested by other researchers on mode I, mode II and mixed-mode I+II loadings [22, 29, 36]. Nevertheless, it should be noted that this set of cohesive parameters was particularly suggested for the T300/HS 160 REM carbon/epoxy composite. For different types of composite systems such as kenaf [37, 38], napier [39, 40], jute and hemp [41], the cohesive parameters are necessary to be evaluated again.

Determination of the Cohesive Zone Length

The length of the first fully developed cohesive zone is defined as the cohesive zone length, $L_{cz,f}$. In other words, the numerical $L_{cz,f}$ refers to the distance between the first element at the crack tip, which experiences total damage ($D = 1$), and the element in the case of which damage initiation is just attained ($D = 0$). It is important to have a sufficient number of cohesive elements in the cohesive zone to ensure accurate simulation results. Hence, the minimum number of cohesive elements, N_e , is another important parameter that is expressed as:

$$N_e = \frac{L_{cz,f}}{l_e} \quad (6)$$

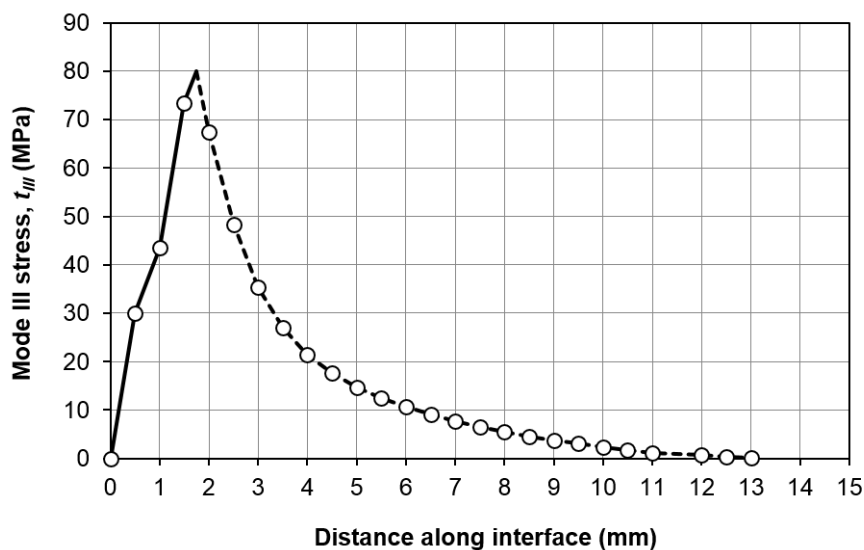


Figure 6. Stress distribution of the first fully developed cohesive zone.

Figure 6 plots the stress distribution of the first fully developed cohesive zone from the results obtained using the suggested cohesive parameters. The peak stress was reasonable to be slightly extrapolated to 80 MPa, which was the interface strength input to the model. It was also the instant where the damage was initiated (Equation (2)). Before the peak load was attained, the element behaved linear elastically according to Equation (1). Beyond that, the damage propagation occurred and the stress decreased progressively according to Equation (4). It is observed that $L_{cz,f}$ was 1.5 mm, which means that there were 3 cohesive elements within the cohesive zone. This is consistent with the recommendations by other researchers, where at least 2-3 cohesive elements are needed in the cohesive zone for accurate simulations [13, 29].

Crack Front and Fracture Process Zone Profiles

The crack front (CF) refers to the region where the cohesive elements have attained total failure ($D = 1$). The fracture process zone (FPZ) is the region where the cohesive elements have experienced damage initiation ($0 \leq D < 1$). Sometimes, it is also known as the cohesive zone. The definition of the damage parameter, D is to be referred to Equation (4). The CF and FPZ contours of the ECT specimen were plotted in Figure 7. It could be seen that the crack propagation was not uniform. This implies the inaccuracy of the assumption of a uniform crack growth between the spheres [25]. Damage was firstly initiated and propagated at the normalised distance of approximately 0.7, which is at the similar region observed by other researchers [25]. At peak load, the crack has propagated ($D = 1$) for approximately 2.8 mm, whereas the damage initiation ($0 \leq D < 1$) has reached 3.2 mm.

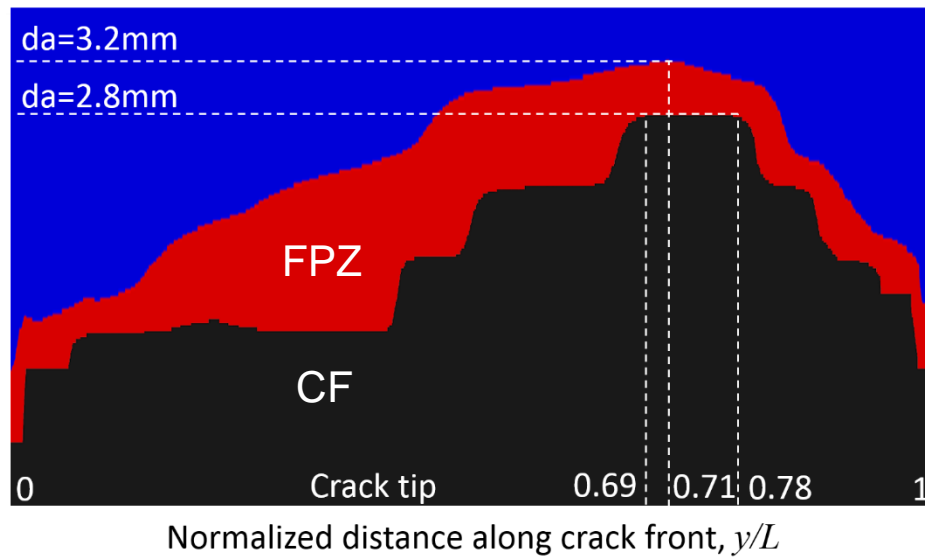


Figure 7. Crack front and fracture process zone along the crack front.

The fracture energy distribution, G_C along the crack front at peak load was presented in Figure 8. To investigate the contribution of each mode in the delamination, the mode II and mode III strains, δ_{II} and δ_{III} at peak load were plotted. It could be noticed that mode III was mainly dominated between the normalised distance of 0.34-0.86. It was in accordance to what has been reported by other researchers, where ECT test has the advantage of having pure mode III in the region between the loading and support pins [5, 14, 15, 17, 25]. In addition, it is worth to note that the normalised location near 0.34 was also the location with the minimal mode II component. The mode II component was larger

than the mode III component at approximately only 1.5% of the normalised distance from the left edge. Hence, it is reasonable to regard the ECT test as a pure mode III fracture toughness test.

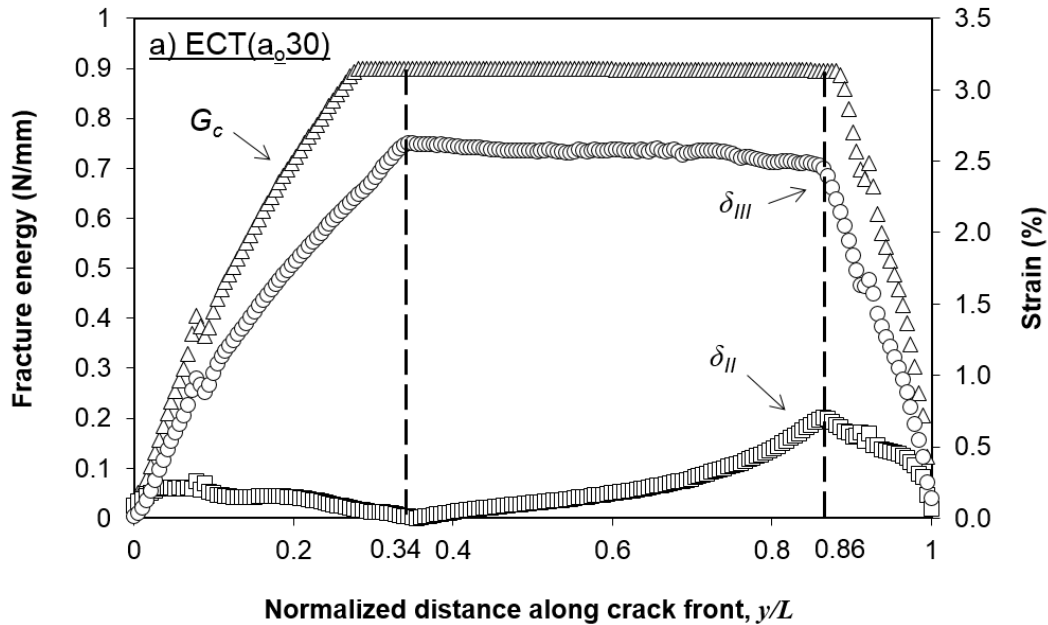


Figure 8. Fracture energy and strain distributions along the crack front

CONCLUSIONS

In this study, the mode III delamination behaviour of an ECT specimen was simulated using cohesive elements. Based on the simulation results from this study, it is proposed that for an accurate simulation of the mode III interlaminar fracture using the ECT specimen at a reasonable computational time, it was suggested to use a 0.5 mm mesh size, which provided three elements in the cohesive zone, interface strength of 80 MPa, viscosity parameter as 1×10^{-3} and interface stiffness with a value of 4×10^6 MPa/mm.

In addition, it was observed that the delamination was started from a normalised location of approximately 0.7 along the crack front. Furthermore, the fracture energy distribution was found to be similar to the fracture process zone (FPZ) contour. Through strain distribution plots, it was also noticed that the delamination in the ECT specimen was mode III dominated. The numerical results from this study have provided a guideline on how to accurately simulate mode III delamination behaviour of an ECT specimen. This study could be further extended to different types of materials and initial crack lengths for the generalisation of the numerical model.

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