

RESEARCH ARTICLE

Statistical analysis, modeling and multi-objective optimization of parameters intermittent turning process of AISI D3

F. Khelfaoui, M. A. Yallese, N. Ouelaa, S. Chihaoui, S. Belhadi

Laboratory of Mechanics and Structure (LMS), Department of Mechanical Engineering, University 8 May 1945, BP 401 Guelma 24000, Algeria Phone: +213 37 10 05 53; Fax: + 213 37 10 05 55

ABSTRACT - Intermittent machining is characterized by its complex and irregular context. This intermittency causes machining to occur under difficult conditions that greatly influence the technological performance parameters. The aim of the present work is to evaluate the effects of input parameters, cutting speed, V_c, depth of cut, a_p, tool nose radius, r and feed rate, f, on surface roughness, Ra, tangential cutting force, Fz, motor power consumption, Pm, cutting power, Pc and material removal rate (MRR), during intermittent turning (IT) of AISI D3 tool steel. Machining was performed with a triple CVD coated carbide tool (Al₂O₃/TiC/TiCN) by adopting a Taguchi L9 (3⁴) experimental design. The ANOVA and RSM methods were used to analyze the effects of cutting factors on the outputs parameters resulting in statistical prediction models. In addition, a multi-objective optimization of the cutting conditions exploiting the desirability function (DF) was done according to four cases of relative importance corresponding to different industrial contexts. Furthermore, the grey relational analysis (GRA) method was applied and compared with the DF method. The results show that the optimal regime found by the DF method, (r =1.6mm, V_c = 240 m/min, f = 0.084 mm/rev and a_p = 0.64 mm), favors Ra and MRR. On the other hand, for the GRA method, the combination of (r = 0.4 mm, $V_c = 240$ m/min f = 0.08 mm/rev and $a_p = 0.3$ mm) favors the minimization of F_z , P_m and Pc. This work presents an originality because the results found are very useful in the field of optimization for a better control of the process IT.

ARTICLE HISTORY

Received	:	07th Dec. 2022
Revised	:	23 rd Mar. 2023
Accepted	:	29th Mar. 2023
Published	:	28th June 2023

KEYWORDS

Intermittent turning Machinability Power consumption Modelling Optimization

1.0 **INTRODUCTION**

The machining operation encompasses several different technological parameters, and the control of all of them is an industrial goal that depends on the context of machining, the machined material, and the number of factors studied [1, 2]. The discontinuous geometry of the part, the specific mechanical properties of the material, as well as its industrial destinations, impose additional difficulties on the manufacturer. Intermittent turning of materials is considered difficult machining, characterized by its complex and irregular context. This intermittent causes machining under severe conditions that greatly influence the technological performance parameters [3]. The exploitation of modeling and optimization methods is very effective for studying this kind of machining operation that can offer the desired interest to industrialists [4].

In this context of IT machining, several research works have been carried out. Ko et al. [5] conducted a study on the IT of bearing steel made of AISI 52100 to evaluate the performance of CBN cutting tools with different nitride contents. The output factors V_B , R_a , and F_z were monitored. The results prove that increasing the nitride content induces a decrease in R_a and V_B . Liu et al [6] performed experiments in IT of 2.25Cr1Mo0.25V steel with two different cutting tools of YT5 and GC4235. The obtained results showed that the tool performance GC4235 is superior to the tool YT5. Liu et al [7] conducted experiments in IT on 2.25Cr-1Mo-0.25V material with a coated carbide tool GC4235. Empirical models of MRR and F_z parameters as a function of V_c, a_p, and f were proposed. Also, at low cutting speeds, abrasive wear and spalling were the main wear mechanisms; however, at high speeds, coating delamination and adhesive wear are prevalent. Carou et al [8] examined the effects of feed rate, MQ lubrication and type of workpiece interruption on vibration during Intermittent machining of UNS M11917 magnesium alloy using an uncoated carbide tool. F. Gong et al [9] conducted an experimental study in IT of 20CrMnTi hardened steel using Al₂O₃-TiC ceramic. The cutting forces and failure mechanisms of the cutting tools were evaluated as a function of varying cutting conditions. An experimental investigation was performed by Cui et al [10] to identify the optimal cutting parameters in the IT of AISI 1045 steel using an Al₂O₃/(W, Ti)C ceramic cutting tool. The results found allowed for an optimal area of surface roughness, cutting energy, and specific energy consumed using finite element method (FEM) as the optimization method.

Recently, Kudryashova et al. [11] conducted experimental study in IT, in order to understand the stabilization of cutting tools on complex surfaces. The analysis of the results showed that Ra is improved by 20% to 70% if a tool with a damping element in IT replaces the standard tool. In addition, Nayak et al. [12] performed a comparison between CT and

IT of AISI D6 tool steel using a tool with low CBN content. The results found in IT show that V_c does not affect the cutting forces, and the wear mechanisms are abrasion and diffusion.

On the other hand, AISI D3 high-alloy steel has been the subject of several experimental studies that focus on machinability, MQ lubrication, tool wear, modeling, and optimization of cutting conditions [13-20]. Also, the desirability function approach is among the multi-objective optimization methods extensively used in many industrial sectors because of the advantages it presents [21-28]. Several researchers have adopted the GRA method as a multi-objective optimization method for cutting conditions due to its effectiveness in making the right decision for selecting the optimal parameters [29-35].

The review of the previous literature clearly shows that intermittent turning presents a case study frequently encountered in the industry, and this particular case of machining deserves special attention in order to evaluate, model, and optimize the technological performance parameters. Also, the particularity of this work lies in the fact that little investigation has been carried out on the intermittent turning of AISI D3 steel by considering the particular intermittent form on the workpiece and by considering four factors of input and four factors of output technical characteristics. Add to this, a comparison of the optimal cutting regimes obtained by two distinct optimization methods of DF and GRA.

The present work aims to evaluate the technological performance parameters namely R_a , F_z , P_m , P_c and MRR as a function of cutting conditions r, V_c , a_p , and f of AISI D3 steel in IT context. ANOVA was used to quantify the influence of input factors on the responses. The statistical treatment of the results allowed us to propose prediction models in IT. Two multi-objective optimization methods were performed by exploiting the DF and GRA approaches according to objectives frequently found in the industry. The results found are of primary importance to researchers working on multi-objective optimization problems of operating factors during intermittent machining.

2.0 EXPERIMENTAL PROCEDURE

2.1 Machined Material and Cutting Tool

The material of study is high-alloy steel AISI D3, intended for cold work with a very high resistance to abrasive wear, medium toughness, dimensional stability, and high resistance to compression. This material has a wide application in the industrial field, such as in machining and forming tools such as punches, and rolling mills, as well as the manufacture of measuring instruments such as gauges, stamps, and gauges [25]. The chemical composition of AISI D3 steel is shown in Table 1. The workpiece used in turning tests is 185 mm in length and 70 mm in diameter. In order to ensure intermittent turning us made three bearings over a length of 85 mm, the width of the groove is 3.33 mm. A cutting insert composed of eight cutting edges made of triple-coated metal carbide (Al₂O₃/TiC/TiCN) of the Sandvik brand GC4215 was used for IT tests as shown in Figure 1. It is mounted on a tool holder on ISO designation PSBNR 2525M12 with geometry represented by γ =-6°, α =-6°, and χ r=75°. For each machining operation, the cutting tool undergoes three (3) shocks successively.

Table 1. Chemical composition of AISI D3 steel									
Composition	С	Si	Ni	Mo	Mn	S	Р	Cu	Cr
Percentage (%)	2	0.31	0.259	0.124	0.29	0.009	0.011	0.162	12



Figure 1. Cutting tool; (a) coating layer, (b) cutting insert and (c) tool holder

2.2 Measuring Devices and Experimental Design

Intermittent turning experiments were performed on a Tos Trencin SN40C brand lathe with 6.6 kW of power, following the standard ISO 3685. The lathe is equipped with a variable speed drive, model ABB series ACS355, with a speed sensor allowing the control of spindle speed. The value of the R_a criterion was measured with a roughness tester model MITUTOYO SJ-210 as shown in Figure 2(a), 2(b) and 2(c). It consists of a 5-µm diamond tip feeler that moves axially over a distance of 4 mm with a cut-off λ = 0.8 mm on the machined surface. The measurement is repeated three times, following an angular position of 120° for each test. The tangential cutting force F_z, was recorded in real time using a Kistler dynamometer type 9257 B, as can be seen in Figure 2(d), 2(e) and 2(f). Figures 2(g), 2(h) and 2(i) show the measurement of motor power consumption, P_m using a LUTRON DW-6095 three-phase power analyzer in real time throughout the intermittent machining operation. The entire experimental procedure is shown in Figure 2. In order to

investigate the influence of the selected input parameters on the targeted response parameters, a L9 (3^4) Taguchi experimental design was chosen to reduce the cost of the experiments and simplify the experimental protocol. The operating conditions chosen to perform the experiments and the values of the cutting parameters are organized in Tables 2 and 3.



Figure 2. Equipment and materials

Table 2. Op	perational	conditions
-------------	------------	------------

Elements	Description
Lathe	SN40C (6.6 kW)
Workpiece	AISI D3
Cutting tool	AI203/TiC /TiNC Carbide insert (CVD)
Tool holder	SANDVIK PSBNR 2525M 12

Table 3.	Cutting	conditions
----------	---------	------------

Elements	Description	Values		
	Cutting speed (V _c)	240; 280; 320 (m/min)		
T	Feed rate (f)	0.08; 0.12; 0.16 (mm/rev)		
Input parameters	Depth of cut (a _p)	0.3 ; 0.6 ; 0.9 (mm)		
	Nose raduis (r)	0.4 ; 1.2 ; 1.6 (mm)		
Output parameters	R_a ; F_z ; P_m ; P_c ; MRR	-		
Cutting procedure	Intermittent turning	-		
Lubrication	Dry	-		

2.3 Cutting Power and Material Removal Rate

The cutting power consumed, P_c in the machining operations, is a very important indicator to follow, because of its impact on the final cost of a product [36]. This indicator deserves to be evaluated in order to minimize it in the optimization studies. In our case the P_c , is calculated according to Eq. (1) based on the measured value of the F_z .

$$P_c = \frac{F_Z \times V_C}{60} \quad \text{(Watt)} \tag{1}$$

The material removal rate, MRR is a factor that represents productivity [37]. Which calculated by following equation.

$$MRR = \frac{V_c \times a_p \times f \times 10^3}{60} \qquad (\text{mm}^3/\text{s})$$
(2)

3.0 RESULTS AND DISCUSSION

3.1 Experimental Results

The results of the tests performed according to the Taguchi L9 design (3⁴) are collected and organized in Table 4. These results obtained represent the response parameters: R_a , F_z , P_m , P_c , and MRR as a function of the input parameters r, V_c , a_p , and f. It appears from the results that the R_a varies from 0.825 μ m to 1.201 μ m. F_z varies between 42.23 N and 240.45 N; P_m varies from 2900 to 4900 Watt. P_c varies between 168.92 Watt and 1282.40 Watt and finally the MRR varies from 96 mm³/s to 768 mm³/s. Figure 3 shows the profile of the cutting forces components in IT. The F_z component has been considered in this work because it is preponderant than F_x and F_y . Figure 4 shows the P_m profile during intermittent turning.

	Table 4. Experimental results											
			Input Factor		Resp	onses						
N°	r (mm)	V _c (m/min)	f (mm/rev)	a _p (mm)	R_a (μm)	$F_z(N)$	P _m (Watt)	P _c (Watt)	MRR (mm ³ /s)			
1	0.4	240	0.08	0.3	0.867	42.23	2900	168.92	96			
2	0.4	280	0.12	0.6	1.034	145.69	3652	679.89	336			
3	0.4	320	0.16	0.9	1.201	240.45	4900	1282.40	768			
4	1.2	240	0.12	0.9	0.934	155.85	3912	623.40	432			
5	1.2	280	0.16	0.3	1.060	142.36	3804	664.35	224			
6	1.2	320	0.08	0.6	0.873	145.25	4120	774.67	256			
7	1.6	240	0.16	0.6	0.938	178.19	3932	712.76	384			
8	1.6	280	0.08	0.9	0.825	162.53	4355	758.47	336			
9	1.6	320	0.12	0.3	0.878	110.62	4100	589.97	192			



Figure 3. Cutting forces profile in IT



Figure 4. Motor power profile in IT

3.2 ANOVA of Performances

ANOVA results of R_a, F_z, P_m and P_c responses are exposed in Table 5. The abbreviations for the values reported in Table 4 are, Dof is degrees of freedom, SumSqr is sum of squares, Cont % is percentage contribution of each factor, SumSq adjusted is adjusted sum of squares; MS adjusted is adjusted mean squares. F is the Fisher value and p is the probability value. If the value of p is less than 0.05, the input parameter is considered significant [38]. Surface roughness ANOVA results reveal that the two input parameters f and r possess a great influence with cont% of 57.86% and 29.63% respectively, followed by V_c with a cont% of 6.53%, however a_p is non-significant with a cont% of 3.46%. These results are in agreement with those of D. Carou et al. [39]. a_p and f, are the main factors having the greatest influence on F_z , their cont% is 51.82% and 33.19% respectively. The V_c factor comes in third place with a cont% of 10.75%, while r is nonsignificant P > 0.05 with a cont% of 0.41%. Gong et al [9] reported similar results, Cui et al. [40], Ni et al [41] indicating that the increase of both factors ap and f causes the increase of effort Fz. From the ANOVA of Pm, it is obvious that all the input factors are significant; V_c and a_p have the major influence, with a cont% of 40.37% and 39.93% respectively. They are followed by f and r, which have cont% of 11.37% and of 5.79% respectively. The results of P_c indicate that the factors V_c , f and a_p are significant, with cont% of 39.50%, 33.45% and 23.51% respectively. However, the r is insignificant with a contribution of 0.15%. A comparable study by Safi et al [25] indicated that the factors V_c and a_p are the first responsible factors on the increase of P_c. For the ANOVA of the MRR, it has not been treated, since it is a parameter calculated by equation no. 2 as a function of the input factors. This equation will be exploited in the optimization study.

Figure 5 summarizes the contribution of each cutting factor on the response parameters, and ANOVA error. It is clear from this figure that a_p is the factor with the most significant effect on the three parameters F_z , P_m and P_c with contributions that exceed the value of 39%, while for the parameter R_a , the factor f has the greatest dominance with a contribution of over 57%. Figure 6 plots the main effects of the output parameters R_a , F_z , P_m , and P_c as a function of variations in the input factors r, V_c , f, and a_p . The factor with the largest slope has the greatest influence on the output parameter under study; the figure confirms that a_p has a strong signification on F_z , P_m and P_c . Also, V_c and f have impact on all output parameters under study. Finally, the factor r particularly has the largest slope on the graph R_a , compared to the other output parameters.

Source	Dof	Sum sqr	Cont %	Sumsqr adjusted	MS adjusted	F value	p value		
(R_a)									
r	1	0.034304	29.63%	0.034304	0.034304	46.96	0.002		
Vc	1	0.007562	6.53%	0.007561	0.007561	10.35	0.032		
f	1	0.066993	57.86%	0.066993	0.066993	91.70	0.001		
a _p	1	0.004004	3.46%	0.004004	0.004004	5.48	0.079		
Error	4	0.002922	2.52%	0.002922	0.000731				
Total	8	0.115784	100.00%						
				(F _z)					
r	1	90.8	0.41%	90.8	90.8	0.42	0.551		
Vc	1	2402.0	10.75%	2402.0	2402.0	11.21	0.029		
f	1	7419.5	33.19%	7419.5	7419.5	34.63	0.004		
a _p	1	11582.6	51.82%	11582.6	11582.6	54.07	0.002		
Error	4	856.9	3.83%	856.9	214.2				
Total	8	22351.8	100.00%						
				(P _m)					
r	1	134979	5.79%	134979	134979	9.14	0.039		
Vc	1	940896	40.37%	940896	940896	63.73	0.001		
f	1	265020	11.37%	265020	265020	17.95	0.013		
a _p	1	930628	39.93%	930628	930628	63.04	0.001		
Error	4	59053	2.53%	59053	14763				
Total	8	2330577	100.00%						
				(P _c)					
r	1	966	0.15%	966	966	0.18	0.697		
Vc	1	217345	33.45%	217345	217345	39.47	0.003		
f	1	152784	23.51%	152784	152784	27.75	0.006		
a _p	1	256694	39.50%	256694	256694	46.62	0.002		
Error	4	22026	3.39%	22026	5507				
Total	8	649815	100.00%						

Table 5. ANOVA of Ra, Fz, Pm and Pc



Figure 5. Input factor contribution: (a) Pm, (b) Ra, (c) Fz and (d) Pc



Figure 6. Main effects graphs for: (a) Pc, (b) Ra, (c) Pm and (d) Fz

3.3 Response Modelling

Modeling the output parameters of a technological process presents an important task because it allows prediction [42]. Generally, the prediction models found are of significant interest in the optimization stage of cutting conditions [43], [44]. In our case study, the relationship between the output responses and the input factors was established by linear regression equations, presented as mathematical models Eq. (3) to Eq. (6) with a different \mathbb{R}^2 .

$$R_a = 0.4715 - 0.1238 r + 0.000888 V_c + 2.642 f + 0.0861 a_p \qquad (R^2 = 97.48)$$
(3)

$$F_z = -193.2 + 146.5 a_p + 879 f + 0.500 V_c + 6.37 r \qquad (R^2 = 96.1)$$
(4)

$$P_m = -488 + 245.5 r + 9.90 V_c + 5254 f + 1313 a_p \qquad (R^2 = 97.47)$$
(5)

$$P_c = -1508 - 20.8 r + 4.758 V_c + 3989 f + 689 a_n$$
 (R²=96.61) (6)

Eq. (3) to Eq. (6) have been exploited to plot the response surfaces 3D as well as the contours for the studied response parameters, taking into account the two most influential input parameters, illustrated in Figure 7. In addition, the contour plots represent a capital interest because they allow one to estimate the value of the studied output parameter according to the combination of the two chosen input factors [45].



Figure 7. 3D Graphs and contours of Ra, Fz, Pm and Pc

The studied performances R_a , F_z , P_m , and P_c are represented by graphs of the response surfaces and contours according to the two most influential input parameters. The reading of the response surface and contour graphs clearly shows that an increase of f causes a degradation of the machined surface quality translated by the increase of the quality index Ra, because the increase of feed rate creates helical grooves due to the translational movement of the cutting tool and the rotation of the workpiece simultaneously. The larger f is, the wider and deeper the helical grooves became. However, increasing r leads to an improvement in surface quality. This is due to the smoothing phenomenon of the machined surface that occurs when r increases. As the depth of cut increases, the cutting surface in contact with the tool also increases, which increases the force required to cut the material. This results in an increase in F_z . Therefore, an increase in feed rate per revolution f results in an increase in cutting force, F_z , this is because f is directly related to the amount of material the tool must remove MRR. An increase in f means that the tool must remove more material, which results in an increase in cutting force, F_z . It is obvious that an increase in cutting speed leads to an increase in cutting power, P_c . The same way the increase of a_p causes the increase of P_c because the power is directly related to the cutting force, which is justified in our case where the increase of a_p induces an increase of F_z , and this increase of F_z generates in parallel an increase of P_c . Moreover, as long as P_c is part of the power of the engine P_m , this imperatively induces that any increase of the power, P_c necessarily causes an increase of P_m .

3.4 Multi-Objective Optimization

Due to the severe competition and rivalry in the global market between mechanical manufacturing companies. Also, to meet the requirements of customers in terms of quality, productivity and final cost of the product, multi-objective optimization of performance parameters has become a primary objective of several researchers [45]. In this work, we have exploited two approaches; DF approach based on the mathematical models found and GRA which is part of MCDM method family. The goal is to propose one or more optimal cutting combinations of cutting parameters according to the different desired objectives. We point out here that the comparison between the two approaches DF and GRA was limited only to the case where all the output parameters have the same importance.

3.4.1 Desirability function

The method is widely used in solving multi-objective optimization problems because of its simplicity and effectiveness in putting in the hands of the users the best solutions for choosing the cutting parameters that ensure the global objective aimed at. DF with the value closest to 1 indicates the optimal combination of cutting parameters [46]. It is given by the following equations:

$$Des(y) = \begin{cases} 0 & y < Low \\ \left(\frac{y - Low}{Tar - Low}\right)^{W} & Low \le y \le Tar \\ 1 & y > Tar \end{cases}$$
(7)

$$Des(y) = \begin{cases} 1 & y < Tar\\ \left(\frac{Up - y}{UP - Tar}\right)^{W} & Tar \le y \le Up\\ 0 & y > Up \end{cases}$$
(8)

$$Des_{comb} = (Des1 \ x \ Des2 \ x \ \dots \ x \ Desn \ x \ Desn \)^{\frac{1}{n}} = \left(\prod_{i=1}^{n} Des_{i}\right)^{\frac{1}{n}}$$
(9)

In this study, four optimization cases favoring the choice of optimal cutting conditions during intermittent machining of AISI D3 are considered. In Table 6, the constraints of the optimization, the desired objectives as well as the importance chosen for the output parameters, which varies from 1 to 5 according to fourth studied cases, are recorded.

	Table 6. Optimization constraints and importance									
		Values	s (V)			Importance				
Pa	rameters	<i>(p)</i>	<i>(p)</i>	Objective	1^{st}	2^{nd}	$\mathcal{3}^{rd}$	4^{th}		
		Lower	Upper		Case	Case	Case	Case		
	r	0.4	1.6		-	-	-	-		
out	Vc	240	320	Level V Com	-	-	-	-		
Inf	f	f 0.08 0.16	$low \leq v \leq up$	-	-	-	-			
	a _p	0.3	0.9		-	-	-	-		
	R _a	0.825	1.201	Minimize	5	5	5	5		
Ħ	Fz	42.23	240.45	Minimize	1	1	5	1		
utpı	\mathbf{P}_{m}	2900	4900	Minimize	1	5	5	1		
0	Pc	168.92	1282.40	Minimize	1	1	5	1		
	MRR	96	768	Maximize	1	5	5	5		

Table 6 Optimization constraints and importance

Table 7 shows the final solutions obtained by DF approach. These solutions include the optimal cutting regime, the corresponding optimized outputs, and the desirability value for the four optimization cases considered. These found solutions meet the manufacturers' objectives during the machining operation of IT parts made of D3 steel. In the first optimization case, R_a takes the maximum value of importance of 5; on the other hand, the other parameters take a minimum importance of 1. The objective is to have an excellent surface finish that meets the requirements of a customer who prefers first-order surface quality [47]. This is a finishing operation, where R_a must be minimized. The optimal regime that corresponds to this machining operation is shown in Table 7 with a minimum roughness R_a equal to 0.825 μ m and a desirability of 0.754. The second optimization case considers a maximum importance of (5) attributed to the three performance parameters R_a , P_m and MRR, however F_z and P_c take a minimum importance equal to 1. This optimization case is interesting in the case of mass production, when the desired objective is to seek a compromise between minimizing R_a , P_m and maximizing productivity. The optimized output parameters take the values 0.887 μ m, 3665.08 Watt, and 309.145 mm³/s for R_a , P_m , and MRR respectively, with a desirability of 0.556. For the third

optimization case, an importance of 5 is assigned to the five performance parameters in order to minimize R_a , F_z , P_m , P_c and maximize the MRR. A trade-off between all outputs is sought in this optimization case. The optimal regime is proposed in Table 7 with a found desirability of 0.603. The fourth optimization case aims at maximum productivity and surface quality simultaneously [48]. An importance of 5 is assigned to the parameters R_a and MRR, while an importance of 1 is assigned to the remaining parameters. This case study is interesting for a customer who is only interested in quality and productivity while energy consumption is in last order. The optimized outputs take the values 0.908 μ m and 404.918 mm³/s for R_a and MRR respectively, with a desirability of 0.560.

In conclusion, we can say that the choice of an optimal cutting speed in the context of intermittent machining depends on the objective. Either the search for maximum surface quality, maximum productivity, minimum energy consumption, minimum production cost of machined parts or also, the combination of one, two or all the objectives together [23, 49-51].

Table 7. Selected solutions										
		Input	factors			Out	put parame	ters		Dec
	r	V_{c}	a _p	f	Ra	$\mathbf{F}_{\mathbf{z}}$	$\mathbf{P}_{\mathbf{m}}$	Pc	MRR	Des
1 st case	1.6	240	0.57	0.087	0.825	91.50	3359.08	310.94	200.59	0.754
2nd case	1.6	240	0.71	0.109	0.887	130.99	3665.08	494.12	309.15	0.556
3rd case	1.6	240	0.64	0.084	0.846	95.98	3376.43	330.74	216.01	0.603
4 th case	1.6	240	0.71	0.143	0.908	168.53	4003.51	670.97	404.92	0.56

3.4.2 GRA method

The GRA method belongs to the family of methods MCDM [52], it is suitable for solving multi-objective problems. In our case it is applied for the optimization of cutting conditions in intermittent machining with the aim of maximizing the MRR and minimizing the performance parameters R_a , F_z , P_m and P_c simultaneously. The GRA method is based on the steps illustrated in Figure 8. In this study, the operation of GRA method is performed by setting the same objectives as the third optimization case studied by DF, which is interested in optimizing the five performance parameters simultaneously with equal importance. Hereunder the GRA steps, the equations used for the calculations, and the meanings of each term in the equations [53]. The results obtained are organized in Table 8.



Figure 8. Steps of GRA method

Step 1: Normalization of results

$$x_i(k) = \frac{max\left(x_i^0(k)\right) - x_i^0(k)}{max\left(x_i^0(k)\right) - min\left(x_i^0(k)\right)}$$
 Lower is better (10)

$$x_i(k) = \frac{x_i^0(k) - \min\left(x_i^0(k)\right)}{\max\left(x_i^0(k)\right) - \min\left(x_i^0(k)\right)}$$
 Greater is better (11)

where, $x_i(k)$: normalized value; $x_i^0(k)$: result value; $max(x_i^0(k))$:max value of (k^{th}) response $x_i^0(k) min(x_i^0(k))$: min value of (k^{th}) response $x_i^0(k)$.

Step 2: Grey relational coefficient (GRC)

$$GRC = \frac{\Delta_{min} + \beta \Delta_{max}}{\Delta_{0i} + \beta \Delta_{max}}$$
(12)

$$\Delta_{0i}(k) = \|x_0(k) - x_i(k)\|$$
(13)

where, Δ_{0i} (k): deviation sequence, difference in absolute value between x_0^k (k) and x_i^k (k)

 Δ_{min} : The lowest value of $\Delta_{0i}(k)$; Δ_{max} : the highest value of $\Delta_{0i}(k)$

 β : Identification coefficient defined in the range $0 \le \beta \le 1$ in our case, the value of β is 0.5.

Step 3: Grey relational grade (GRG)

$$GRG = \frac{1}{n} \sum_{k=1}^{n} GRC \tag{14}$$

where, n: is the number of tests.

Step 4: Selection of the optimum parameters

Classification of grg values in descending order, the largest grg value has the best range of optimal parameters.

Step 5: GRA confirmation test

$$\gamma_i = \gamma_m + \sum_{i=1}^{p} (\overline{\gamma_i} - \gamma_m) \tag{15}$$

where, γ_m : is the total mean grg; $\overline{\gamma_i}$: is the mean grg at the optimal level; p: is the number of major variables.

Table 8 shows the coefficients and ranks of the Gray Relation for each experiment in the Taguchi L9 design. Applying the instructions in step 4, it is clearly observed that the trial number 1 has the largest GRG value of 0.830, the optimal regime proposed by this method is that of experiment number 1: r = 0.4 mm, $V_c = 240$ m/min, f = 0.08mm/rev, $a_p = 0.3$ mm. The Figure 9 presents the graph of the main effects of GRG according to the variations of the input factors r, V_c , f and a_p . Table 9 shows the responses of GRG averages, the factor with largest Delta value has greatest influence on GRG.

Table 8. GRC and GRG results										
No.			GRC			CPC	Donk			
Exp	Ra	$\mathbf{F}_{\mathbf{z}}$	\mathbf{P}_{m}	Pc	MRR	UKU	Kalik			
1	0.817	1.000	1.000	1.000	0.333	0.830	1			
2	0.474	0.489	0.571	0.521	0.438	0.499	7			
3	0.333	0.333	0.333	0.333	1.000	0.467	9			
4	0.633	0.466	0.497	0.551	0.500	0.529	4			
5	0.444	0.497	0.525	0.529	0.382	0.476	8			
6	0.797	0.490	0.450	0.479	0.396	0.523	5			
7	0.625	0.422	0.492	0.506	0.467	0.502	6			
8	1.000	0.452	0.407	0.486	0.438	0.556	2			
9	0.780	0.592	0.455	0.569	0.368	0.553	3			



Table 9. Responses for GRG

Parameters —		GRG		Delta	Domin
	Level 1	Level 2	Level 3	Max-Min	Kalik
r	0.5984	0.5091	0.5371	0.0893	4
V_{c}	0.6205	0.5102	0.5140	0.1104	3
f	0.6364	0.5269	0.4815	0.1549	1
\mathbf{a}_{p}	0.6195	0.5077	0.5175	0.1118	2

3.4.3 Comparison between DF and GRA Optimization

The results obtained with the two multi-objective optimization methods are summarized in Table 10. The purpose of this comparison is to establish the performance of each method and to leave the choice to the industrialists to decide the application of this or that approach. It is clear that the DF favors the parameters of surface quality and productivity at the same time, where the roughness is minimal, and productivity is maximal $R_a = 0.846\mu$ m and MRR=216.01mm³/s. On the other hand, the factors F_z , P_m , and P_c take maximum values. On the other hand, the GRA proposes an optimal regime favoring the minimization of cutting force F_z by a percentage of 56.00% compared to the DF, as well as a minimization of energy consumption of 14.11% and 48.93% for P_m and P_c respectively. The surface quality value $R_a=0.867\mu$ m found is almost comparable to that found by DF with a small increase of 2.48% only, however the productivity parameter is very low MRR=96 mm³/s which is a strong decrease of 55.56% compared to DF. Finally, both methods propose to the industrialists two optimal regimes with the same cutting speed $V_c = 240$ m/min, and almost the same feed rate f=0.08 mm/rev while the two factors r and a_p are totally different.

Table 10. Results of DF and GRA methods

	Input factors				Output parameters				
	r	Vc	f	a _p	R _a	F_z	\mathbf{P}_{m}	Pc	MRR
	(mm)	(m/min)	(mm/rev)	(mm)	(µm)	(N)	(Watt)	Watt)	(mm^{3}/s)
DF	1.6	240	0.084	0.64	0.846	95.98	3376.43	330.74	216.01
GRA	0.4	240	0.08	0.3	0.867	42.23	2900	168.92	96
Difference (%)	-75.00	0.00	-4.76	-53.05	2.48	-56.00	-14.11	-48.93	-55.56

3.5 Relationship between Motor Power and Cutting Power

For the realized experimental design, the change of the cutting conditions for different tests generates different values of P_c and P_m . Figure 10 shows the histogram of the recorded values of P_c and P_m . The ratios (P_m/P_c) for the 9 tests performed are as follows: {17.17; 5.37; 3.82; 6.28;5.73; 5.32; 5.52; 5.74; 6.95}. The power P_c is included in the total power consumed by the motor P_m . Figure 11 shows the histogram of the percentages of P_c versus $(P_m - P_c)$ for each test performed.



Figure 10. Pm and Pc for each test



Figure 11. Rate of Pc and Pm-Pc

4.0 CONCLUSION

The present work concerns an experimental study of modeling and multi-objective optimization of cutting parameters during intermittent machining of AISI D3 steel using DF and GRA methods. The results of the ANOVA of R_a show that the factors f and r have the greatest impact on R_a , while the ANOVA of F_z reveals that a_p and f have the greatest influence. However, the ANOVA of Pm and P_c clearly shows that V_c and a_p are the most dominant factors. In addition, the mathematical models found for R_a , F_z , P_m and P_c in the context of intermittent turning are accurate, with high R^2 ranging from 96.1% to 97.48%. These models are very useful for prediction and optimization.

Multi-objective optimization of cutting conditions by applying the DF method to four well-defined cases, which meet industrial requirements, offers the possibility of choosing the optimum solution according to the desired case. The comparison of the optimal regimes found by the DF and GRA methods is of great industrial interest, as it enables the correct selection of the optimal regimes that correspond to the targeted objectives. The DF method gives the best results for minimizing R_a and maximizing MRR. The GRA method, on the other hand, favours minimization of F_z , P_m and P_c , while maintaining surface quality very close to that of the DF method.

5.0 ACKNOWLEDGEMENT

The present research was undertaken by the "Metal Cutting Research Group" of the (LMS) Laboratory of the 8 May 1945-Guelma University, Algeria. The work is funded by LMS Laboratory of the 8 May 1945-Guelma University, Algeria and (DGRSDT) under the PRFU research projects A11N01UN240120220002-A11N01UN240120230001.

6.0 **REFERENCES**

- D. Carou, E. M. Rubio, C. H. Lauro, L. C. Brandão, and J. P. Davim, "Study based on sound monitoring as a means for superficial quality control in intermittent turning of magnesium workpieces," *Procedia CIRP*, vol. 62, pp. 262-268, 2017.
- [2] E. M. Rubio, M. Villeta, B. de Agustina, and D. Carou, "Surface roughness analysis of magnesium pieces obtained by intermittent turning," in *Materials Science Forum*, vol. 773, pp. 377-391, 2014.
- [3] X. Cui and J. Guo, "Identification of the optimum cutting parameters in intermittent hard turning with specific cutting energy, damage equivalent stress, and surface roughness considered," *The International Journal of Advanced Manufacturing Technology*, vol. 96, pp. 4281-4293, 2018.
- [4] C. Camposeco-Negrete, "Optimization of cutting parameters for minimizing energy consumption in turning of AISI 6061 T6 using Taguchi methodology and ANOVA," *Journal of Cleaner Production*, vol. 53, pp. 195-203, 2013.
- [5] T. Ko and H. Kim, "Surface integrity and machineability in intermittent hard turning," *The International Journal of Advanced Manufacturing Technology*, vol. 18, pp. 168-175, 2001.
- [6] H. L. Liu, X. Lv, C. Z. Huang, Z. B. Yin, B. Zou, and H. T. Zhu, "Tools optimization in efficient Intermittent cutting of 2.25 Cr1Mo0. 25V Steel," in Advanced Materials Research, vol. 188, pp. 469-474, 2011.
- [7] H. L. Liu, X. Lv, C. Z. Huang, and H. T. Zhu, "Experimental study on intermittent turning 2.25 Cr-1Mo-0.25 V steel with coated cemented carbide tool," in *Advanced Materials Research*, vol. 500, pp. 128-133, 2012.
- [8] D. Carou, E. Rubio, C. Lauro, and J. Davim, "The effect of minimum quantity lubrication in the intermittent turning of magnesium based on vibration signals," *Measurement*, vol. 94, pp. 338-343, 2016.
- [9] F. Gong, J. Zhao, and J. Pang, "Evolution of cutting forces and tool failure mechanisms in intermittent turning of hardened steel with ceramic tool," *The International Journal of Advanced Manufacturing Technology*, vol. 89, pp. 1603-1613, 2017.

- [10] X. Cui, J. Guo, and J. Zheng, "Optimization of geometry parameters for ceramic cutting tools in intermittent turning of hardened steel," *Materials & Design*, vol. 92, pp. 424-437, 2016.
- [11] E. Kudryashov, I. Smirnov, E. Yatsun, and N. Khizhnyak, "Stabilizing tool for intermittent turning of complex surfaces," *Russian Engineering Research*, vol. 39, pp. 141-146, 2019.
- [12] M. Nayak, R. Sehgal, and R. Kumar, "Investigating machinability of AISI D6 tool steel using CBN tools during hard turning," *Materials Today: Proceedings*, vol. 47, pp. 3960-3965, 2021.
- [13] M. Yallese, J. Rigal, K. Chaoui, and L. Boulanouar, "The effects of cutting conditions on mixed ceramic and cubic boron nitride tool wear and on surface roughness during machining of X200Cr12 steel (60 HRC)," *Proceedings of the Institution of Mechanical Engineers, Part B: Journal of Engineering Manufacture,* vol. 219, no. 1, pp. 35-55, 2005.
- [14] H. Bouchelaghem, M. Yallese, T. Mabrouki, A. Amirat, and J. F. Rigal, "Experimental investigation and performance analyses of CBN insert in hard turning of cold work tool steel (D3)," *Machining Science and Technology*, vol. 14, no. 4, pp. 471-501, 2010.
- [15] M. Nouioua, M. A. Yallese, R. Khettabi, S. Belhadi, and T. Mabrouki, "Comparative assessment of cooling conditions, including MQL technology on machining factors in an environmentally friendly approach," *The International Journal of Advanced Manufacturing Technology*, vol. 91, pp. 3079-3094, 2017.
- [16] V. Shinge and M. Pable, "Effect of nano-minimum quantity lubrication on cutting temperature and surface roughness of milling AISI D3 tool steel," *Materials Today: Proceedings*, vol. 72, pp. 1758-1764, 2023.
- [17] K. Safi, M. A. Yallese, S. Belhadi, S. Boutabba, and T. Mabrouki, "Optimisation multi-objective des paramètres de coupe lors de l'usinage d'un acier pour travail à froid avec un carbure revêtu CVD (Al2O3/TiC/TiCN)," UPB Scientific Bulletin, Series D: Mechanical Engineering, vol. 83, no. 1, pp. 149-168, 2021.
- [18] M. Uzun, Ü. A. Usca, M. Kuntoğlu, and M. K. Gupta, "Influence of tool path strategies on machining time, tool wear, and surface roughness during milling of AISI X210Cr12 steel," *The International Journal of Advanced Manufacturing Technology*, vol. 119, no. 3-4, pp. 2709-2720, 2022.
- [19] A. M. M. Ibrahim, M. A. Omer, S. R. Das, W. Li, M. S. Alsoufi, and A. Elsheikh, "Evaluating the effect of minimum quantity lubrication during hard turning of AISI D3 steel using vegetable oil enriched with nanoadditives," *Alexandria Engineering Journal*, vol. 61, no. 12, pp. 10925-10938, 2022.
- [20] A. Naghashzadeh, A. Shafyei, and F. Sourani, "Nanoindentation and tribological behavior of TiN-TiCN-TiAlN multilayer coatings on AISI D3 tool steel," *Journal of Materials Engineering and Performance*, vol. 31, no. 6, pp. 4335-4342, 2022.
- [21] D. K. Mohanta, B. Sahoo, and A. M. Mohanty, "Optimization of process parameter in AI7075 turning using grey relational desirability function and metaheuristics," *Materials and Manufacturing Processes*, pp. 1-11, 2023.
- [22] S. K. Kar, P. K. Mishra, A. K. Sahu, S. S. Mahapatra, and J. Thomas, "Multi-objective optimization of wire-EDM of Inconel 625 by using desirability function approach," *International Journal on Interactive Design and Manufacturing (IJIDeM)*, pp. 1-8, 2023.
- [23] A. Zerti, M. A. Yallese, O. Zerti, M. Nouioua, and R. Khettabi, "Prediction of machining performance using RSM and ANN models in hard turning of martensitic stainless steel AISI 420," *Proceedings of the Institution of Mechanical Engineers, Part C: Journal of Mechanical Engineering Science*, vol. 233, no. 13, pp. 4439-4462, 2019.
- [24] S. Chihaoui, M. A. Yallese, S. Belhadi, A. Belbah, K. Safi, and A. Haddad, "Coated CBN cutting tool performance in green turning of gray cast iron EN-GJL-250: modeling and optimization," *The International Journal of Advanced Manufacturing Technology*, vol. 113, pp. 3643-3665, 2021.
- [25] K. Safi, M. A. Yallese, S. Belhadi, T. Mabrouki, and S. Chihaoui, "Parametric study and multi-criteria optimization during turning of X210Cr12 steel using the desirability function and hybrid Taguchi-WASPAS method," *Proceedings of the Institution of Mechanical Engineers, Part C: Journal of Mechanical Engineering Science*, vol. 236, no. 15, pp. 8401-8420, 2022.
- [26] A. H. Jawad, U. K. Sahu, N. A. Jani, Z. A. ALOthman, and L. D. Wilson, "Magnetic crosslinked chitosantripolyphosphate/MgO/Fe3O4 nanocomposite for reactive blue 19 dye removal: Optimization using desirability function approach," *Surfaces and Interfaces*, vol. 28, p. 101698, 2022.
- [27] J.-S. Cho, D.-H. Lee, G.-J. Seo, D.-B. Kim, and S.-J. Shin, "Optimizing the mean and variance of bead geometry in the wire+ arc additive manufacturing using a desirability function method," *The International Journal of Advanced Manufacturing Technology*, vol. 120, no. 11-12, pp. 7771-7783, 2022.
- [28] A. Perec, "Desirability function analysis (DFA) in multiple responses optimization of abrasive water jet cutting process," *Reports in Mechanical Engineering*, vol. 3, no. 1, pp. 11-19, 2022.

- [29] A. Hamdi and S. M. Merghache, "Application of artificial neural networks (ANN) and gray relational analysis (GRA) to modeling and optimization of the material ratio curve parameters when turning hard steel," *The International Journal of Advanced Manufacturing Technology*, pp. 1-14, 2023.
- [30] A. Venkata Vishnu and S. Sudhakar Babu, "Mathematical modeling & multi response optimization for improving machinability of alloy steel using RSM, GRA and Jaya algorithm," *International Journal of Engineering*, vol. 34, no. 9, pp. 2157-2166, 2021.
- [31] P. Wu, Y. He, Y. Li, J. He, X. Liu, and Y. Wang, "Multi-objective optimisation of machining process parameters using deep learning-based data-driven genetic algorithm and TOPSIS," *Journal of Manufacturing Systems*, vol. 64, pp. 40-52, 2022.
- [32] R. R. Panigrahi, A. Panda, A. K. Sahoo, R. Kumar, and R. R. Mishra, "Turning performance analysis and optimization of processing parameters using GRA-PSO approach in sustainable manufacturing," *Proceedings of the Institution of Mechanical Engineers, Part E: Journal of Process Mechanical Engineering*, vol. 236, no. 6, pp. 2404-2419, 2022.
- [33] A. Venkata Vishnu, S. S. Babu, and P. J. Kumar, "Multi-response optimization of machining characteristics using MQL through GRA and TOPSIS approach," in *Sustainable Machining Strategies for Better Performance: Select Proceedings of SMSBP 2020*, 2022, pp. 23-37, 2022.
- [34] V. R. Balwan, B. Dabade, and B. B. Kabnure, "Optimization of surface finish and material removal rate while turning hardened EN 353 steel using GRA," *Materials Today: Proceedings*, vol. 59, pp. 331-338, 2022.
- [35] K. Safi, M. A. Yallese, S. Belhadi, T. Mabrouki, and A. Laouissi, "Tool wear, 3D surface topography, and comparative analysis of GRA, MOORA, DEAR, and WASPAS optimization techniques in turning of cold work tool steel," *The International Journal of Advanced Manufacturing Technology*, vol. 121, no. 1-2, pp. 701-721, 2022.
- [36] M. Trifunović, M. Madić, P. Janković, D. Rodić, and M. Gostimirović, "Investigation of cutting and specific cutting energy in turning of POM-C using a PCD tool: Analysis and some optimization aspects," *Journal of Cleaner Production*, vol. 303, p. 127043, 2021.
- [37] S. Y. Martowibowo, I. Ariza, and B. Damanik, "Comparison of metal removal rate and surface roughness optimization for AISI 316L using sunflower oil minimum quantity lubrication and dry turning processes," *Journal* of Mechanical Engineering and Sciences, vol. 16, no. 3, pp. 8976-8986, 2022.
- [38] A. Hamza, K. Bousnina, and N. B. Yahia, "An approach to the influence of the machining process on power consumption and surface quality during the milling of 304L austenitic stainless steel," *Journal of Mechanical Engineering and Sciences*, vol. 16, no. 3, pp. 9093-9109, 2022.
- [39] D. Carou, E. Rubio, C. Lauro, and J. Davim, "Experimental investigation on surface finish during intermittent turning of UNS M11917 magnesium alloy under dry and near dry machining conditions," *Measurement*, vol. 56, pp. 136-154, 2014.
- [40] X. B. Cui, J. Zhao, Y. H. Zhou, and Z. Pei, "Cutting forces and tool wear in intermittent turning processes with Al₂O₃-based ceramic tools," in *Key Engineering Materials*, vol. 499, pp. 205-210, 2012.
- [41] X. Ni, J. Zhao, F. Wang, F. Gong, X. Zhong, and H. Tao, "Failure analysis of ceramic tool in intermittent turning of hardened steel," *Proceedings of the Institution of Mechanical Engineers, Part B: Journal of Engineering Manufacture*, vol. 232, no. 12, pp. 2140-2153, 2018.
- [42] U. M. R. Paturi, A. Yash, S. T. Palakurthy, and N. Reddy, "Modeling and optimization of machining parameters for minimizing surface roughness and tool wear during AISI 52100 steel dry turning," *Materials Today: Proceedings*, vol. 50, pp. 1164-1172, 2022.
- [43] B. Eskandari, S. Bhowmick, and A. T. Alpas, "Turning of Inconel 718 using liquid nitrogen: multi-objective optimization of cutting parameters using RSM," *The International Journal of Advanced Manufacturing Technology*, vol. 120, no. 5-6, pp. 3077-3101, 2022.
- [44] P. Anggoro, Y. Purharyono, A. A. Anthony, M. Tauviqirrahman, and A. Bayuseno, "Optimisation of cutting parameters of new material orthotic insole using a Taguchi and response surface methodology approach," *Alexandria Engineering Journal*, vol. 61, no. 5, pp. 3613-3632, 2022.
- [45] S. A. Bagaber and A. R. Yusoff, "Multi-objective optimization of cutting parameters to minimize power consumption in dry turning of stainless steel 316," *Journal of cleaner production*, vol. 157, pp. 30-46, 2017.
- [46] O. Benkhelifa, A. Cherfia, and M. Nouioua, "Modeling and multi-response optimization of cutting parameters in turning of AISI 316L using RSM and desirability function approach," *The International Journal of Advanced Manufacturing Technology*, vol. 122, no. 3-4, pp. 1987-2002, 2022.
- [47] Ü. A. Usca *et al.*, "Tool wear, surface roughness, cutting temperature and chips morphology evaluation of Al/TiN coated carbide cutting tools in milling of Cu–B–CrC based ceramic matrix composites," *Journal of Materials Research and Technology*, vol. 16, pp. 1243-1259, 2022.

- [48] A. T. Abbas, A. A. Al-Abduljabbar, I. A. Alnaser, M. F. Aly, I. H. Abdelgaliel, and A. Elkaseer, "A closer look at precision hard turning of AISI4340: multi-objective optimization for simultaneous low surface roughness and high productivity," *Materials*, vol. 15, no. 6, p. 2106, 2022.
- [49] D. R. Shah, N. Pancholi, H. Gajera, and B. Patel, "Investigation of cutting temperature, cutting force and surface roughness using multi-objective optimization for turning of Ti-6Al-4 V (ELI)," *Materials today: proceedings*, vol. 50, pp. 1379-1388, 2022.
- [50] B. Li, X. Tian, and M. Zhang, "Modeling and multi-objective optimization method of machine tool energy consumption considering tool wear," *International Journal of Precision Engineering and Manufacturing-Green Technology*, vol. 9, pp. 127-141, 2022.
- [51] S. P. Anand and A. K. Saraf, "Optimization of surface roughness and material removal rate in turning of AISI D3 steel with coated carbide inserts," in *IOP Conference Series: Materials Science and Engineering*, vol. 1224, no. 1, p. 012010, 2022.
- [52] A. El-Araby, I. Sabry, and A. El-Assal, "A comparative study of using MCDM methods integrated with entropy weight method for evaluating facility location problem," *Operational Research in Engineering Sciences: Theory and Applications*, vol. 5, no. 1, pp. 121-138, 2022.
- [53] D. Mukherjee, R. Ranjan, and S. Moi, "Multi-response optimization of surface roughness and MRR in turning using Taguchi Grey Relational Analysis (TGRA)," *International Research Journal of Multidisciplinary Scope* (*IRJMS*), vol. 3, pp. 1-7, 2022.